#### Baryon Acoustic Oscillations

Vicent J. Martínez (Valencia University)

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# Outline

- 0 Introduction. Correlation function and power spectum
  - Physics of Baryon Acoustic Oscillations (BAO)
  - BAO previous detections
  - Oetection and Reconstruction of Baryon Acoustic Structures







# **Correlation Analysis**

# The two-point correlation function

Infinitesimal interpretation:

 $dP_{12} = \overline{n}^2 [1 + \xi(\mathbf{r})] dV_1 dV_2$ 

is the joint probability that in each one of the two infinitesimal volumes  $dV_1$  and  $dV_2$ , with separation vector **r**, lies a galaxy.

# **Spatial Correlation Function**

- Totsuji & Kihara (1969)
  - Spatial correlation function of galaxies

Clustering pattern of galaxies, as a function of scales

### Matsubara



$$dP = \overline{n}^2 dV_1 dV_2 \left[ 1 + \xi(r) \right]$$

Probability of having galaxies in both cells

Spatial correlation function



#### The Correlation Function for the Distribution of Galaxies

Hiroo Totsuji and Taro Kihara

Department of Physics, Faculty of Science, University of Tokyo (Received May 15, 1969; revised June 26, 1969)

#### Abstract

The correlation function for the spatial distribution of galaxies in the universe is determined to be  $(r_0/r)^{1.8}$ , r being the distance between galaxies. The characteristic length  $r_0$  is 4.7 Mpc. This determination is based on the distribution of galaxies brighter than the apparent magnitude 19 counted by SHANE and WIRTANEN (1967). The reason why the correlation function has the form of inverse power of r is that the universe is in a state of "neutral" stability.

Number of data pairs with separation rNumber of random pairs with separation r





FIG. 2. Comparison of the empirical and theoretical values of  $\frac{\langle \{N_1 - \langle N \rangle\} \{N_2 - \langle N \rangle\} \rangle}{\langle \{N - \langle N \rangle\}^2 \rangle - \langle N \rangle}$ . The filled circles indicate the empirical values obtained by the authors, and the open circles and crosses by NEYMAN et al.; the unit solid angle is  $1^{\circ} \times 1^{\circ}$  for the circles and  $10' \times 10'$  for the crosses. The curves are theoretical values for s=1.7, 1.8, 1.9, and 2.0.

# **Estimators**

### Minus estimator

For galaxies close to the boundary the number of neighbors is obviously underestimated. One way to overcome this problem is to consider as centers for counting neighbors only galaxies lying within an inner window  $W_{\rm in}$ ; then we can average

$$\hat{\xi}_{\min}(r) = rac{V(W)}{NN_{\mathrm{in}}} \sum_{i=1}^{N_{\mathrm{in}}} rac{n_i(r)}{V_{\mathrm{sh}}} - 1,$$

where  $V_{\rm sh}$  is the volume of the shell of width dr.





Edge-corrected estimarors

$$\hat{\xi}_{\text{RIV}}(r) = rac{V(W)}{N^2} \sum_{i=1}^{N} rac{n_i(r)}{V_i} - 1,$$

 $n_i(r)$  is the number of neighbors at distance in the interval [r, r+dr] from galaxy *i*,  $V_i$  is the volume of the intersection of the shell with *W*. When *W* is a cube, an analytic expression for  $V_i$  is provided in Baddeley et al. (1993) *Appl. Statis.*, 42, 641.

$$\xi_N = \frac{N_r(N_r - 1)}{N_d(N_d - 1)} \frac{DD}{RR} - 1$$

$$\xi_{LS} = \frac{\frac{N_r(N_r - 1)}{N_d(N_d - 1)}DD - \frac{N_r - 1}{N_d}DR + RR}{RR}.$$

# The Galaxy Correlation Function

- First measured by Totsuji and Kihara, then Peebles et al
- Mostly angular correlations in the beginning
- Later more and more redshift space
- Power law is a good approximation

$$\xi(r) = \left(\frac{r}{r_0}\right)^2$$

- Correlation length  $r_0 = 5.4$  h<sup>-1</sup> Mpc
- Exponent is around  $\gamma = 1.8$
- Corresponding angular correlations

$$w(\theta) = \left(\frac{\theta}{\theta_0}\right)^{1-1}$$

### (From A. Szalay)



**Figure 3.** The non-parametric estimates of the real-space correlation functions are shown for both our spectral types, using the method of Saunders, Rowan-Robinson & Lawrence (1992). It can be seen that our assumption of a power law form for  $\xi(r)$  is justified out to scales of up to 20  $h^{-1}$  Mpc. The solid lines are the best-fitting power law fits shown in Table 1, whereas the dashed lines are extrapolations of these fits.

Madgwick et al., 2004 (2dFGRS)

# Power Spectrum

# Quantification of Clustering Structures in 1-D

Long-wavelength

Larger amplitude/power

Short-wavelength

smaller amplitude/power

# Quantification of Clustering

This distribution has a lot of long wavelength power And a little short wavelength power





3. LOS RUIDOS BLANCOS Y ROSAS nos rodean. El ruido

# Match up the power spectra from Sarah Bridle



Courtesy of David Kirkby - UC Irvine

# The Power Spectrum

The power spectrum of a function y(x) is:

$$P(\vec{k}) = \left| \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{+\infty} y(\vec{x}) \exp(-i\vec{k} \cdot \vec{x}) d\vec{x} \right|^2$$
$$= \tilde{y}(\vec{k})\tilde{y}(\vec{k})^*$$

 remember that y(x) is a particular realization of some random field φ(x)



units are [length]<sup>-3</sup>

# **Power spectrum**

### Real space

Correlation function:

$$E\left\{\rho(\mathbf{x})\rho(\mathbf{x}+\mathbf{r})\right\} = \bar{\rho}^2 \left[1 + \xi(\mathbf{r})\right].$$

Density contrast:

$$\delta(\mathbf{x}) = \frac{\rho(\mathbf{x}) - \bar{\rho}}{\bar{\rho}},$$
$$E\left\{\delta(\mathbf{x})\delta(\mathbf{x} + \mathbf{r})\right\} = \xi(\mathbf{r})$$

## Fourier space (advantages)

- It is more intuitive physically, separating processes on different scales.
- Theoretical model predictions are made in terms of power spectrum.
- The amplitudes for different wavenumbers are statistically orthogonal

$$E\left\{ \widetilde{\delta}(\mathbf{k})\widetilde{\delta}^{\star}(\mathbf{k}') \right\} = (2\pi)^{3}\delta_{D}(\mathbf{k} - \mathbf{k}')P(\mathbf{k}).$$

is the Fourier amplitude of the overdensity field  $\boldsymbol{d}$  at a wavenumber  $\boldsymbol{k}$ 

Power spectrum — correlation function:

$$P(\mathbf{k}) = \int \xi(\mathbf{r}) e^{i\mathbf{k}\cdot\mathbf{r}} \, d^3r,$$

Fourier transform pair

$$\xi(\mathbf{r}) = \int P(\mathbf{k})e^{-i\mathbf{k}\cdot\mathbf{r}} \frac{d^3k}{(2\pi)^3},$$

Isotropy:

$$\xi(r) = 4\pi \int_0^\infty P(k) \frac{\sin(kr)}{kr} \frac{k^2 \, dk}{(2\pi)^3}.$$

Delta-power:

$$\Delta^2(k) = \frac{1}{2\pi^2} P(k)k^3,$$

#### (Courtesy of D. Eisenstein)

#### Sound Waves in the Early Universe

#### Before recombination:

- Universe is ionized.
- Photons provide enormous pressure and restoring force.
- Perturbations oscillate as acoustic waves.

#### After recombination:

- Universe is neutral.
- Photons can travel freely past the baryons.
- Phase of oscillation at t<sub>rec</sub> affects late-time amplitude.





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### Waine Hu web page http://background.uchicago.edu/~whu/intermediate/gravity.html

### Gravity tries to compress the fluid in potential wells.

The photon-baryon fluid is sitting in the gravitational potential wells that are the seeds of structure in the universe. As gravity tries to compress the fluid, radiation pressure resists resulting in acoustic oscillations. Because it acts to resist compression, we will represent the radiation pressure abstractly as springs. Likewise we will represent the inertia of the fluid, or loosely speaking its mass (really energy density), as massive balls falling under gravity:



• Sound speed:

$$c_s = c / \sqrt{3(1+R)}$$

$$R = 3\rho_b / 4\rho_\gamma = \delta\rho_b / \delta\rho_\gamma$$

Before recombination, baryons and radiation form a fluid undergoing acoustic oscillations.

After decoupling, baryons are free and have nearly no pressure, so they fall to the potential wells of dark matter.

# Evolution of matter profile from a central perturbation before recombination



- Before recombination, baryons and photons are coupled forming a plasma
- Density fluctuations produce sound waves in the plasma
- At recombination ( $t \sim 380,000$  years), baryons decouple from photons  $\rightarrow$  sound waves become 'frozen' $\rightarrow$  imprint a characteristic 'acoustic' scale in the matter distribution  $r_s = \int_0^{t_{\rm rec}} c_s(t)(1+z) dt \simeq 150 {\rm Mpc}$

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### Evolution of matter profile from a central perturbation



# Physics of BAO: Galaxy Distribution

Evolution of matter profile from a central perturbation after recombination



Massive 'bump' at the centre + spherical shell at r ~ 150 Mpc
 Width of shell related to Silk scale

Physics of BAO: individual perturbation

We study the evolution of the density around a single initial perturbation  $\rightarrow$  A shell of matter will form around the initial perturbation



Images from D. Eisenstein's webpage:

# Physics of BAO: Galaxy Distribution

Average over all the perturbations...



Image from Daniel Eisenstein

Physics of BAO: Cosmic Microwave Background

Evolution of matter profile from a central perturbation before recombination



Baryon Acoustic Oscillations detected in the anisotropies of the CMB

# Physics of BAO: Cosmic Microwave Background

# Evolution of matter profile from a central perturbation before recombination



Baryon Acoustic Oscillations detected in the anisotropies of the CMB



Image Credit: E.M. Huff, the SDSS-III team, and the South Pole Telescope Team. Graphic by Zosia Rostomian



Galaxy map 3.8 billion years ago

Galaxy map 5.5 billion years ago

CMB 13.7 billion years ago

#### BAO in $\xi(r)$ and P(k)

The BAO produce a peak in the correlation function  $\equiv$  a series of oscillations in the power spectrum



- The characteristic scale in ξ(r) or P(k) (r<sub>s</sub>) can be used as a "standard ruler" to constrain the geometry of the universe
- First detected (Eisenstein et al., 2005) in the ξ(r) of SDSS-LRG-DR3 and (Cole et al., 2005) in P(k) of 2dFGRS

# Measuring the Geometry of the Universe

- BAO gives us a standard distance with a fixed comoving value (sound horizon at recombination):
   r<sub>BAO</sub> = 153.3 ± 2.0 Mpc (WMAP5)
- It can be used as a 'ruler' to measure the geometry of the Universe.
  For a flat Universe:
  - Radial:  $dr(z) = \frac{c}{H(z)}dz \rightarrow \Delta z_{BAO} = H(z)r_{BAO}$
  - Angular:  $d_A(z) = \frac{c}{1+z} \int_0^z \frac{dz'}{H(z')} \to \Delta \theta_{BAO} = \frac{r_{BAO}}{d_A(z)}$
- Usually constraint a combination of H(z) and  $d_A(z)$

### Graphic by Zosia Rostomian

# BAO detection in SDSS

First detected  $(3.5\sigma)$  in the  $\xi(r)$  of the Luminous Red Galaxies sample of SDSS [Eisenstein et al. (2005)]



- Confirmed in 2dF and SDSS-photometric at  $\sim 2.5\sigma$
- With lower significance in cluster samples

# LRG samples



Reliability of the detection of BAO in the correlation function

#### Correlation function study: samples used

- Aim: to check reliability of BAO detection in ξ(r) by comparing different samples
- Use largest survey to date (SDSS-LRG, DR7) and 2dFGRS → complementary samples (in terms of density, z, galaxy properties, etc.)



Sample	N	Absolute magnitude	Z	Ω	V	n
		-		(sr)	$(h^{-3}{\rm Gpc}^{3})$	( <i>h</i> <sup>3</sup> Mpc <sup>-3</sup> )
DR7-LRG	92,219	$-23.2 < M_{\sigma}^{0.3} < -21.2$	[0.16, 0.47]	2.02	1.30	$7.1 \times 10^{-5}$
DR7-LRG-VL	41,195	$-23.2 < M_{\sigma}^{0.3} < -21.6$	[0.16, 0.40]	2.02	0.817	$5.0 imes10^{-5}$
2dFVL	32,388	$-21 < \dot{M_{b_{I}}} < -20$	[0.03, 0.19]	0.45	0.024	$1.4  imes 10^{-3}$

Physics of Baryon acoustic oscillations  $O \bullet O$ 

Reliability of the detection of BAO in the correlation function

#### Correlation function study: results

- Estimate ξ(r) using Landy-Szalay method, and errors from block-bootstrap of pair distributions
- BAO peak seen in all three samples  $\rightarrow$  stable feature of the LSS
- Width of peak larger than expected (and previous results)
- Results confirmed with these and other samples (SDSS-Main, 6dFGS, WiggleZ).



# BAO Observational results: cosmological constraintsPercival et al. 2010



Figure 5. Cosmological constraints on  $\Lambda$ CDM cosmologies (upper panel) and flat CDM models where we allow w to vary (lower panel), from WMAP5 (blue), Union SN (green) and our constraint on  $r_s/D_V(0.275)$  (solid contours). Contours are plotted for  $-2 \ln \mathcal{L}/\mathcal{L}_{true} < 2.3$ , 6.0, corresponding to 68 and 95 per cent confidence intervals. The dashed lines show flat models (upper panel) and  $\Lambda$  models (lower panel).

Reconstruction of the baryon acoustic structures

#### Baryon Acoustic Structures reconstruction





Reconstruction of the baryon acoustic structures

#### Baryon Acoustic Structures reconstruction





Reconstruction of the baryon acoustic structures

#### Baryon Acoustic Structures reconstruction



- We recover the 3D shape of the BAO structures  $\Rightarrow$  bump at the centre + spherical shell
- From the radial profile we obtain the radius of the shell,  $r_{\rm shell} = 109.5 \pm 3.9 \ h^{-1} \, {\rm Mpc} \rightarrow {\rm acoustic \ scale}$

## Measuring $\xi(r)$ in photometric redshift surveys

- Large  $\Delta z$  in 'photo-z' catalogues  $\rightarrow$ large uncertainties in position (along line of sight)  $\rightarrow$  can not measure  $\xi(r)$  directly
- Similar problem to redshift-space effects (e.g. finger-of-God) in 'spectro-z' catalogues (but larger effect for 'photo-z')



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• In 'spectro-z' surveys, the projected correlation function method<sup>4</sup> is used to recover  $\xi(r)$ 

Can we use that method for 'photo-z' catalogues?

<sup>4</sup>Davis&Peebles, ApJ **267**, 465 (1983)

Use the DM halo catalogue from the light-cone simulation of Heinämäki et al. (2005) (astro-ph/0507197)

- Simulation covers  $2^{\circ} \times 0.5^{\circ}$  in the sky, standard  $\Lambda CDM$  cosmology
- Study restricted to the redshift bin  $z \in [2,3]$
- Geometry of the volume considered: 864 (line-of-sight)  $\times 160 \times 40$  (transverse)  $h^{-1}$  Mpc
- Total volume:  $4.56 imes 10^6 \, h^{-3} \, \mathrm{Mpc}^3$ ,  $\sim 180,000$  haloes

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z = 3

z = 2

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- Simulated photometric redshift catalogues shifting randomly the (redshift-space) position of haloes along the line-of-sight direction
- We assume Gaussian redshift errors, with  $\Delta z/(1+z)$  constant for each catalogue  $\rightarrow$  valid assumption for 'good' photo-z
- Simulated three 'typical' cases:
  - $\Delta z = 0.05(1+z) \rightarrow$  'classical' broad-band filter survey
  - $\Delta z = 0.015(1+z) \rightarrow$  'good' redshifts with ALHAMBRA
  - $\Delta z = 0.005(1+z) \rightarrow \text{possible future survey (similar to PAU Survey <sup>5</sup>)}$

• Effect of  $\Delta z$ : projection of the different catalogues on a longitudinal plane



Real-space catalogue

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• Effect of  $\Delta z$ : projection of the different catalogues on a longitudinal plane



Redshift space

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• Effect of  $\Delta z$ : projection of the different catalogues on a longitudinal plane



 $\Delta z = 0.005(1+z)$  mock catalogue

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• Effect of  $\Delta z$ : projection of the different catalogues on a longitudinal plane



 $\Delta z = 0.015(1+z)$  mock catalogue

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• Effect of  $\Delta z$ : projection of the different catalogues on a longitudinal plane



 $\Delta z = 0.05(1+z)$  mock catalogue

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## Decomposition of distances and two-dimensional $\xi$

• Decompose distances between pairs of galaxies in transverse ( $\sigma$ ) and line-of-sight ( $\pi$ ).

$$\pi \equiv rac{|\mathbf{s} \cdot \mathbf{I}|}{|\mathbf{I}|} \quad , \quad \sigma \equiv \sqrt{\mathbf{s} \cdot \mathbf{s} - \pi^2}$$

• Can calculate 'two-dimensional'  $\xi(\sigma,\pi) \rightarrow$  count pairs in  $\sigma,\pi$  bins, and use Landy-Szalay estimator



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### Projected correlation function

• Integrate  $\xi(\sigma, \pi)$  along  $\pi \rightarrow$ 'projected correlation function':

$$\Xi(\sigma) = 2 \int_0^\infty \xi(\sigma, \pi) \mathrm{d}\pi$$

- Small angles  $\rightarrow \sigma$  not affected by  $\Delta z \rightarrow \Xi$  not affected by  $\Delta z$
- Have to choose  $\pi_{\max}$  for integration  $\rightarrow$  optimal value  $\pi_{\max} \simeq 4\Delta z$



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## Relation to obtain $\xi(r)$

• Assuming that the (real-space) distribution of galaxies is isotropic  $\rightarrow$  integral relation between  $\Xi(\sigma)$  and  $\xi_r(r)$ 

$$\Xi(\sigma) = 2 \int_{\sigma}^{\infty} \xi_r(r) \frac{r \mathrm{d}r}{\left(r^2 - \sigma^2\right)^{1/2}}$$

• Inverting the relation  $\rightarrow$  obtain  $\xi_r(r)$  in terms of  $\Xi(\sigma)$ :

$$\xi_r(r) = -\frac{1}{\pi} \int_r^\infty \frac{\mathrm{d}\Xi(\sigma)}{\mathrm{d}\sigma} \frac{\mathrm{d}\sigma}{(\sigma^2 - r^2)^{1/2}}$$

Can obtain  $\xi_r(r)$  by numerical integration of  $\Xi(\sigma)$ 

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• Have to choose a  $\sigma_{\max}$  for integration  $\rightarrow$  given by survey geometry

# Why so many filters?



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Large scales again Distortions for expected photometric surveys BAO form photometric redshift surveys

z-space,  $\Delta z = 0.03(1+z) + peculiar velocities$ 

z-space,  $\Delta z =$ 0.003(1+z) + peculiar velocities

z-space, perfect zresolution + peculiar velocities

Real space, perfect resolution





Redshift Diagram J-PAS mock 0.2 < z < 0.4; 0° < b < 5° / A z =0.003





Z



Correlation function J-PAS 0.2 < z < 0.4 (Large scales)





### www.uv.es/martinez



Vicent.Martinez@uv.es